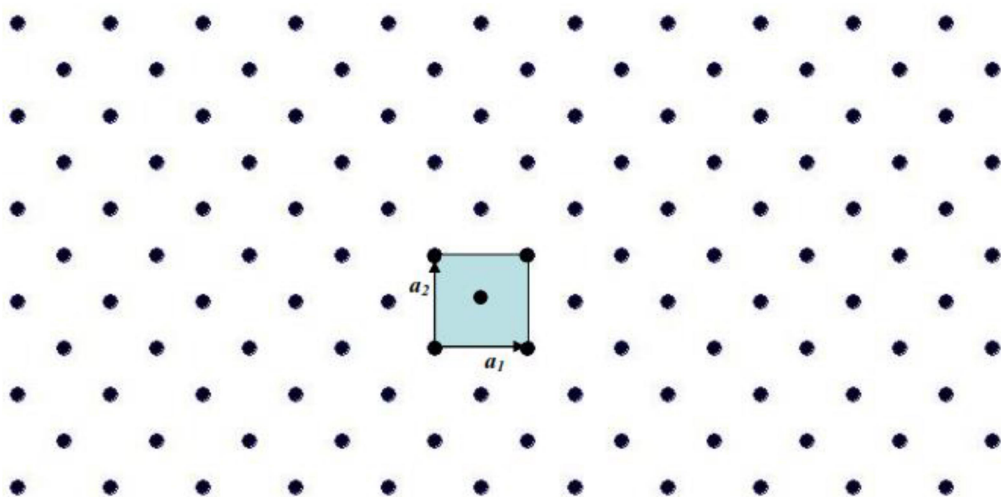
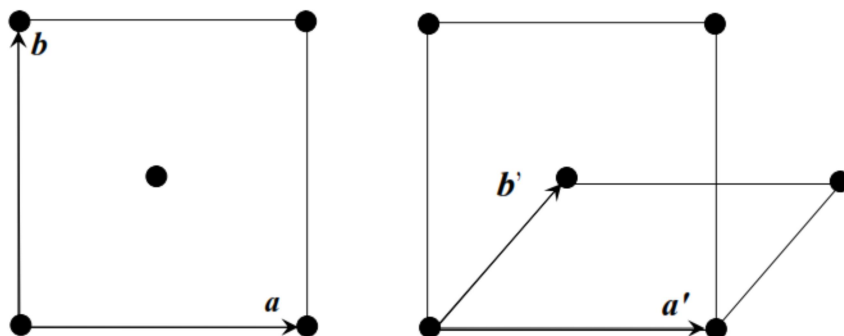


## 6. Homework “Symmetry of crystal lattice, 2D crystal system, 2D Bravais lattice”

1. 2D lattice has two basis vectors  $\mathbf{a}_1$  and  $\mathbf{a}_2$  (see figure below). These vectors have the same size and the angle of  $90^\circ$  in between. The unit cell is non-primitive and contains an additional lattice point at the  $[1/2 \ 1/2]$  position. Which type of a lattice is depicted in the figure, explain why this lattice cannot be a new type of Bravais lattice (No. 6) ?



2. The 2D Bravais lattice (*the centered-rectangular lattice*) can be constructed using the basis vectors of the primitive and non-primitive unit cell accordingly. The basis vector of the primitive unit cell is  $\mathbf{a}' = \mathbf{a}$ ,  $\mathbf{b}' = 1/2\mathbf{a} + 1/2\mathbf{b}$  (see figure below). Find the relation between their reciprocal vectors  $\mathbf{a}^*$ ,  $\mathbf{b}^*$  and  $\mathbf{a}'^*$ ,  $\mathbf{b}'^*$ .



3. Find a type of Bravais lattice using the *Minkowski algorithm* to reduce lattice vectors. The initial vectors  $\mathbf{A}_1$ ,  $\mathbf{A}_2$  and  $\alpha$  angle have the following values:

- a)  $|\mathbf{A}_1|=1$ ,  $|\mathbf{A}_2|=1.6125$ ,  $\alpha = 7.125^\circ$
- b)  $|\mathbf{A}_1|=1$ ,  $|\mathbf{A}_2|=2.0276$ ,  $\alpha = 170.53^\circ$
- c)  $|\mathbf{A}_1|=1$ ,  $|\mathbf{A}_2|=1.5275$ ,  $\alpha = 169.100^\circ$

4. A crystal has the following symmetry elements:

- a) a 2-fold axis  $\parallel \mathbf{e}_1$  and a 4-fold rotoinversion axis  $\parallel \mathbf{e}_3$
- b) a 2-fold axis  $\parallel \mathbf{e}_1$  and a 2-fold axis  $\parallel \mathbf{e}_3$

Find the **complete** symmetry group (all possible symmetry elements) of this crystal.